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Reflection of equatorial Kelvin waves at eastern ocean boundaries

Part II: Pacific and Atlantic Oceans

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Abstract. The effect of viscosity, non linearities, incident wave period and realistic eastern coastline geometry on energy fluxes are investigated using a shallow water model with a spatial resolution of 1/4 degree in both meridional and zonal directions. Equatorial and mid-latitude responses are considered. It is found that (1) the influence of the coastline geometry and the incident wave period is more important for the westward energy flux than for the poleward flux, and (2) the effect of the inclination of the eastern ocean boundary on the poleward energy flux, for the Pacific and Atlantic Oceans, decline as the period of the incident wave increases. Furthermore, the model simulations suggest that the poleward energy fluxes from meridional boundaries give plausible results for motions of seasonal and annual periods. For comparatively shorter periods, a realistic coastline geometry has to be included for more accurate results. It is recommended that any numerical model involving the reflection of baroclinic Rossby waves (of intraseasonal, seasonal or annual periods) on the eastern Pacific or Atlantic Oceans, should consider the effect of the coastline geometry in order to improve the accuracy of the results.

Key words. Oceanography: general (climate and interannual variability; equatorial oceanography). Oceanography: physical (eastern boundary currents).

1 Introduction

Equatorial Kelvin waves are thought to occur over a wide range of frequencies. Sea level records from El Niño years reveal that sustained periods of high sea level

were composed of several wave periods, which were interannually modulated (Madden and Julian, 1971, 1972; Ripa and Haynes, 1981; Enfield, 1989; McPhaden and Taft, 1988; Miller *et al.*, 1988; Glantz *et al.*, 1990; Weickman, 1991; Delcroix *et al.*, 1991; among others). Upon impingement with the eastern boundary, the incoming baroclinic equatorial Kelvin wave excites westward-propagating Rossby waves and poleward-propagating coastal Kelvin waves (Moore, 1968; Moore and Philander, 1977; McCreary, 1976).

The low-frequency response of sea level on the eastern ocean boundaries can be subdivided for linear purposes into two independent constituents (1) the remotely forced part, i.e., that which is the result of an equatorial Kelvin wave incident on the boundary, and (2) the locally forced part. The latter is due to the longshore component of the wind (Bigg and Gill, 1986).

Observational and theoretical studies, however, have indicated that the remotely forced part dominates the sea level variability along the eastern coasts of North and South America, related to the interannual frequency, as in the ENSO phenomenon (Enfield and Allen, 1980; Chelton and Davis, 1982; Pares-Sierra and O'Brien, 1989; Johnson and O'Brien, 1990; Spillane *et al.*, 1986).

In the Atlantic ocean, observations suggest that the upwelling event in the Gulf of Guinea is not associated with either the local winds or the local ocean circulation (Houghton, 1976). A possible explanation is that a strong upwelling signal, generated by increased westward wind stress in the western Atlantic, can travel as an equatorial Kelvin wave (Moore *et al.*, 1978; Adamec and O'Brien, 1978; Servain *et al.*, 1982; Busalacchi and Picaut, 1983; Picaut, 1983; McCreary *et al.*, 1984; Katz, 1987; Verstraete, 1992). This interpretation is analogous to the theories of El Niño in the Pacific ocean.

The nature of the response at an eastern boundary to an incident baroclinic Kelvin wave depends on the latitude, θ , and on the wave period. For low frequencies a critical latitude, θ_c exists such that for $|\theta| < \theta_c$ the response consists of offshore-propagating Rossby

waves, whereas for $|\theta| > \theta_c$ the waves are trapped by the coastal. The magnitude of the critical latitude decreases as the wave period decreases and as the coastline inclination (γ), from meridional orientation, increases. (Grimshaw and Allen, 1988; Clarke and Shi, 1991).

Soares *et al.* (1998) using a viscous baroclinic shallow water model, have investigated the effects of viscosity, non-linearity, angle of coastline inclination and incident wave period on the baroclinic equatorial Kelvin waves at eastern ocean boundaries. They have found, by energy flux considerations, that the impact of viscosity is greater than the effect of non-linearities. A systematic decrease of coastal Kelvin wave energy as the wave period increases (and θ_c increases), predicted by inviscid theories (as in Clarke and Shi, 1991) was not verified in their work, because of the role of energy dissipation in their model. The dissipation was found to be dependent not only on the presence of the coastal Kelvin waves in the domain, but also on the period of these coastal waves. The influence of the angle of coastline inclination and of the incident wave period was found to be more important for the westward energy flux than for the poleward flux.

The main aim of this study is to investigate the behavior of the low-frequency baroclinic equatorial Kelvin waves when they reach the Pacific and Atlantic Ocean eastern coasts. Three different Kelvin wave periods are considered: intraseasonal, seasonal and annual. Some of the questions we address are: how far from the equator can the baroclinic disturbances propagate? How important is the coastline geometry on the propagation of the coastally trapped Kelvin waves and on the generation of the reflected Rossby waves? How important is the viscous effects on the studied waves? Are there differences between propagation in the Northern and Southern Hemispheres of the Pacific and Atlantic Oceans?

2 Numerical model

Non linear, 1/2 layer, shallow-water equations are used as the basis of the numerical model. The model is described in detail in Soares (1994) and Soares *et al.* (1998). Spherical coordinates with λ (longitude) increasing eastward and θ (latitude) increasing northward are used in the model because of its large latitudinal extent. A regular 1/4 degree resolution is used in both zonal and meridional directions ($\Delta\lambda = \Delta\theta = 1/4^\circ$). Linear and nonlinear experiments are performed using a time step (Δt) of 4 and 2 h, respectively. A Laplacian coefficient of $10^3 \text{ m}^2 \text{ s}^{-1}$ is employed in the numerical experiments described in this work. The coefficient value, $10^3 \text{ m}^2 \text{ s}^{-1}$, has been commonly used in baroclinic shallow-water numerical models. Numerically, this coefficient helps to smooth the very high wave number numerical noise. Physically, A_H helps to form a viscous boundary layer required to fit the observations with the theory. The effects of viscosity on linear free baroclinic Kelvin waves in shallow-water models have been discussed by Davey *et al.* (1983) and Hsieh *et al.* (1983).

A modification of Orlanski's (1976) radiative boundary condition (Miller and Thorpe, 1981) was used in all open boundaries: north, south and west. With the present scheme perturbations generated inside the domain are able to cross the artificial boundaries without distortion and without affecting the interior solution. On the solid boundaries the free-slip condition is used.

3 Experiments

The free wave solutions generated by the reflection of a baroclinic Kelvin wave at the eastern Pacific and Atlantic Ocean boundaries is investigated using the numerical model, outlined already with one layer of initial thickness, $H_0 = 200 \text{ m}$. A pulse of finite width is used as surrogate to the baroclinic equatorial Kelvin wave. The maximum amplitude of the initial disturbance is taken as 30 m. From the hydrostatic balance, a 30 m depression of the interface, implies a 10 cm surface elevation (considering $\rho_2 = 1060$ and $\rho_1 = 1025 \text{ Kg m}^{-3}$). The wave meridional structure is assumed to be a Gaussian function of latitude centered on the equator. The linear phase speed is assumed to be 2.45 ms^{-1} . Only half a wavelength of the initial disturbance is used in the experiments.

The eastern Pacific and Atlantic coastlines (Fig. 1) use the contour of 200 m depth line in the boundary calculations instead of the actual coastline, because it is a better approximation of the vertical coast assumed in theory. The initial layer thickness is considered to be 200 m.

To estimate reflection properties it is convenient to consider the energy flux. Outwards along the boundary the energy flux is due to poleward coastal Kelvin waves. Depending on the hemisphere in consideration the poleward energy flux (t_P) can be northward (t_N) or southward (t_S). The net energy flux toward the boundary (t) is given by the difference between the energy fluxes due to the incoming equatorial Kelvin wave (t_E) and due to the reflected Rossby waves (t_W). Therefore, $t_E - t_W = t_N - t_S - t_D$; where t_D is the energy dissipation. It was assumed that the energy flux is positive to the north and east directions.

Three different wave period (as in Soares *et al.*, 1998) are considered: intraseasonal ($T = 60$ days), seasonal ($T = 180$ days) and annual ($T = 360$ days).

In all the experiments, the numerical model is integrated for a time long enough to allow for the coastal Kelvin wave, generated by the equatorial wave to leave the domain.

3.1 Energy flux considerations

The fluxes are numerically calculated considering a region longitudinally bounded by an eastern ocean boundary ($\lambda = \lambda_{\text{coast}}$) and a longitude away from the coast ($\lambda = -\lambda_0$) and latitudinally bounded by $\theta = \pm \theta_0$ (where θ_0 is the latitude in consideration, positive

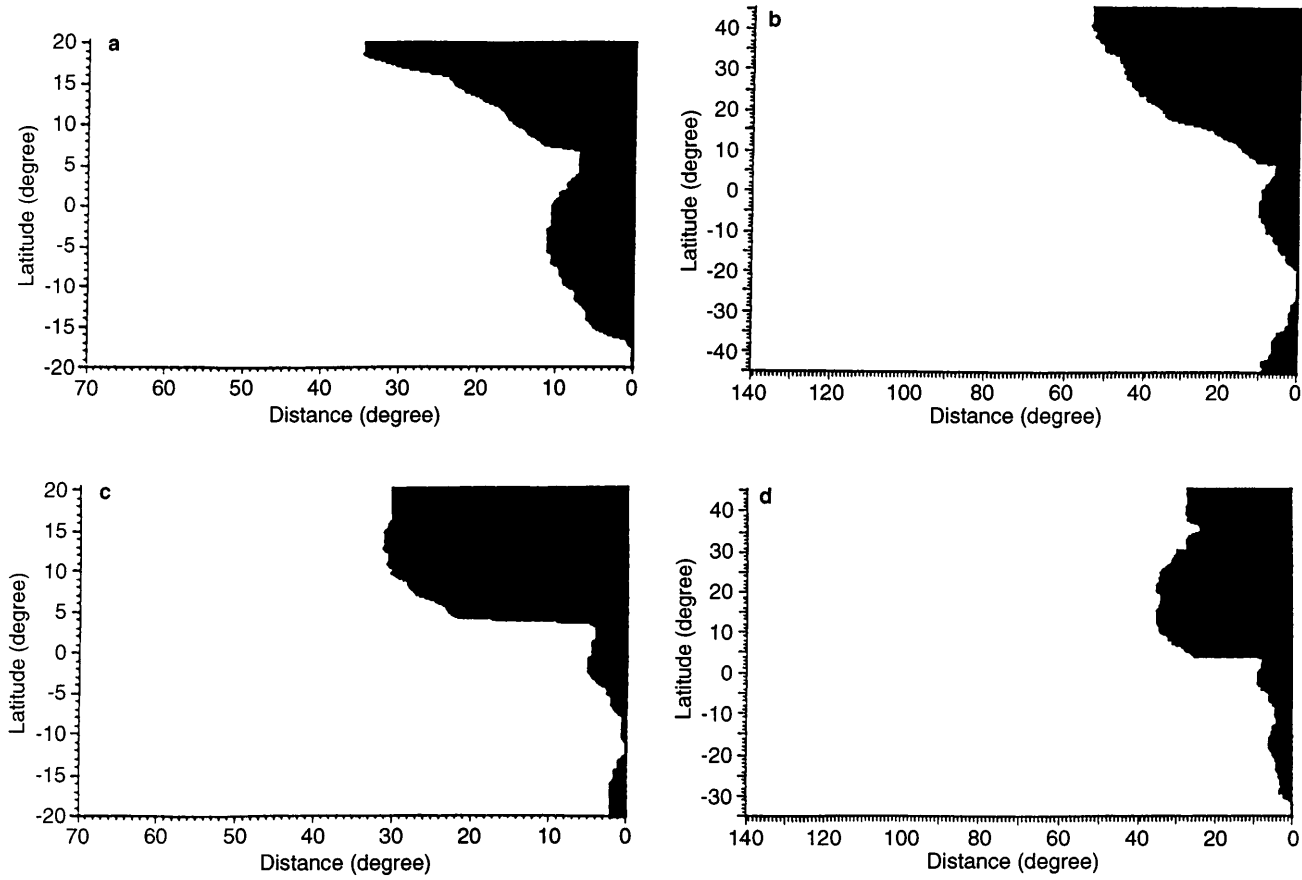


Fig. 1a–d. Model geometry. Pacific Ocean eastern coastline used for the **a** intraseasonal experiment and **b** for the seasonal and annual experiments; Atlantic Ocean eastern coastline used for the **c** intraseasonal experiment and **d** seasonal and annual experiments

northwards). This work assumes that the energy flux due to Kelvin wave can be separated from the one due to Rossby waves. However, in the non linear frame it is not necessarily true.

Poleward energy flux. The poleward energy flux (t_P), across a given latitude $+\theta_0$ is given by:

$$t_{P(\text{linear})} = \sum_{\lambda=-\lambda_0}^{\lambda=\lambda_{\text{coast}}} \overline{g'h H_0 v} r \cos \theta_0 \Delta \lambda \quad (1)$$

$$t_{P(\text{non-linear})} = \sum_{\lambda=-\lambda_0}^{\lambda=\lambda_{\text{coast}}} \overline{(g'h + q)V} r \cos \theta_0 \Delta \lambda \quad (2)$$

where the overbar denotes time average; $h(\lambda, \theta, t)$ is the interface displacement of the upper layer to the mean depth $H_0(\lambda, \theta)$; $u(\lambda, \theta, t)$ and $v(\lambda, \theta, t)$ are the horizontal components of the depth averaged velocity vector $\mathbf{v}(\lambda, \theta, t)$ in the λ (east–east) and θ (north–south) directions, respectively. Reduced gravity is $g' = g(\rho_2 - \rho_1)/\rho_2$, where $g = 9.8 \text{ m/s}^2$ is the acceleration of gravity; ρ_2 e ρ_1 are the density of the upper and lower layers, respectively. The radius of the Earth is taken to be a constant, $r = 6.37 \times 10^6 \text{ m}$; $\mathbf{V}(\lambda, \theta, t) = u\mathbf{H}\mathbf{i} + v\mathbf{H}\mathbf{j} = U\mathbf{i} + V\mathbf{j}$ and $q = (u^2 + v^2)/2$ (kinetic energy per unit of area).

Net energy flux in the east–west direction. The net energy flux (t), toward the boundary across a given longitude $-\lambda_0$, can be given by:

$$t_{(\text{linear})} = t_{E(\text{linear})} - t_{W(\text{linear})} = \sum_{\theta=-\theta_0}^{\theta=+\theta_0} \overline{g'h H_0 u} r \Delta \theta \quad (3)$$

$$t_{(\text{non-linear})} = t_{E(\text{non-linear})} - t_{W(\text{non-linear})} = \sum_{\theta=-\theta_0}^{\theta=+\theta_0} \overline{(g'h + q)U} r \Delta \theta \quad (4)$$

The direct determination of $t = t_E - t_W$, however, is computationally expensive because the propagation speed of the westward Rossby waves is a strong function of the latitude varying from $\sim 0.8 \text{ m/s}$ at the equator to zero at the poles. It could take years of numerical integration for all the Rossby waves, generated at the eastern boundary, to reach the western side of the domain. To save computer time, first t_E is calculated and then t_W is inferred by energy conservation considerations. The energy input in the experiment is only due to the baroclinic equatorial Kelvin wave. Consequently before the reflection of this wave at the eastern coast, the eastward energy flux through a given longitude of the numerical domain corresponds to the value of t_E . It can be assumed that the reflected Rossby wave energy (t_W), for one hemisphere, is given by $t_W/2 = t_E/2 - t_P - t_D/2$.

Energy dissipation. The dissipation of energy (t_D), up to a given latitude $+\theta_0$, can be calculated as:

$$t_{D(\text{linear})} = - \sum_{\lambda=-\lambda_0}^{\lambda=\lambda_{\text{coast}}} \sum_{\theta=0}^{\theta=+\theta} \overline{A_H H_0 (u \nabla^2 u + v \nabla^2 v) r^2 \cos \theta \Delta \theta \Delta \lambda} \quad (5)$$

$$t_{D(\text{non-linear})} = - \sum_{\lambda=-\lambda_0}^{\lambda=\lambda_{\text{coast}}} \sum_{\theta=0}^{\theta=+\theta} \overline{A_H H (u \nabla^2 u + v \nabla^2 v) r^2 \cos \theta \Delta \theta \Delta \lambda} \quad (6)$$

where $H(\lambda, \theta, t)$ is the total depth ($H = H_0 + h$) and ∇^2 is the Laplacian operator in spherical coordinates.

Equations (1), (2), (5) and (6) consider only the Northern Hemisphere. Changing $\theta = +\theta_0$ for $\theta = -\theta_0$ in those expressions gives the Southern Hemisphere fluxes. The energy input is always considered for both Hemispheres and the poleward, westward and energy dissipations are always calculated for the Hemisphere in consideration.

3.2 Model Pacific Ocean results

3.2.1 Intraseasonal variability. In the linear and non linear experiments described in this section the latitudinal model basin extents from -20° to 20° and has a maximum longitudinal extent of 70° . The eastern Pacific boundary approximation used in the intraseasonal experiments can be seen in Fig. 1a.

A baroclinic equatorial Kelvin wave of 60-day period is used as an initial condition of the numerical model for the intraseasonal linear and non linear cases. The numerical model is integrated for 90 days.

The linear northward energy flux (t_N) and the Northern Hemisphere dissipation of energy (t_D) were numerically calculated using Eqs. (1) and (5) respectively; t_S (southward energy flux) and t_D (dissipation) for the Southern Hemisphere were obtained using the same equations but with $\theta = -\theta_0$.

The nondimensional energy flux coefficients (in %) $r_P(\gamma, T)$, $r_W(\gamma, T)$ and $r_D(\gamma, T)$ shown in Fig. 2, are, respectively, the ratios of the poleward (northward or southward depending on the hemisphere) coastal Kelvin wave, of reflected Rossby wave and of the dissipation of energy fluxes to the incoming equatorial Kelvin wave energy flux (i.e., $r_P = t_P/t_E$, $r_W = t_W/t_E$ and $r_D = t_D/t_E$). The coefficients are calculated at latitudinal intervals of 2° and integrated in time for 90 days.

To investigate the effect of the nonlinear terms on low frequency wave reflection at the Pacific boundary, the non linear model is run using the same parameters and the same initial condition as used for the linear case. The non linear poleward coastal Kelvin wave energy flux (t_P) and the dissipation of energy (t_D) are estimated, for both-hemispheres, using Eqs. (2) and (6).

Figure 2a shows the westward energy fluxes calculated using (1) the Pacific coastline and the linear model (PAC-L); (2) meridional coastline and the linear model (CO-L); (3) Pacific coastline and the non linear model (PAC-NL) and (4) meridional coastline and the non linear model (CO-NL).

Figure 2 shows the westward flux (Fig. 2a), poleward flux (Fig. 2b) and dissipation coefficient (Fig. 2c). It can be seen that the changes in energy fluxes and in energy dissipation induced by the coastline geometry are notably more important than those induced by the nonlinearities.

For the cases investigated, and within the confines of this model, the linear and nonlinear poleward energy

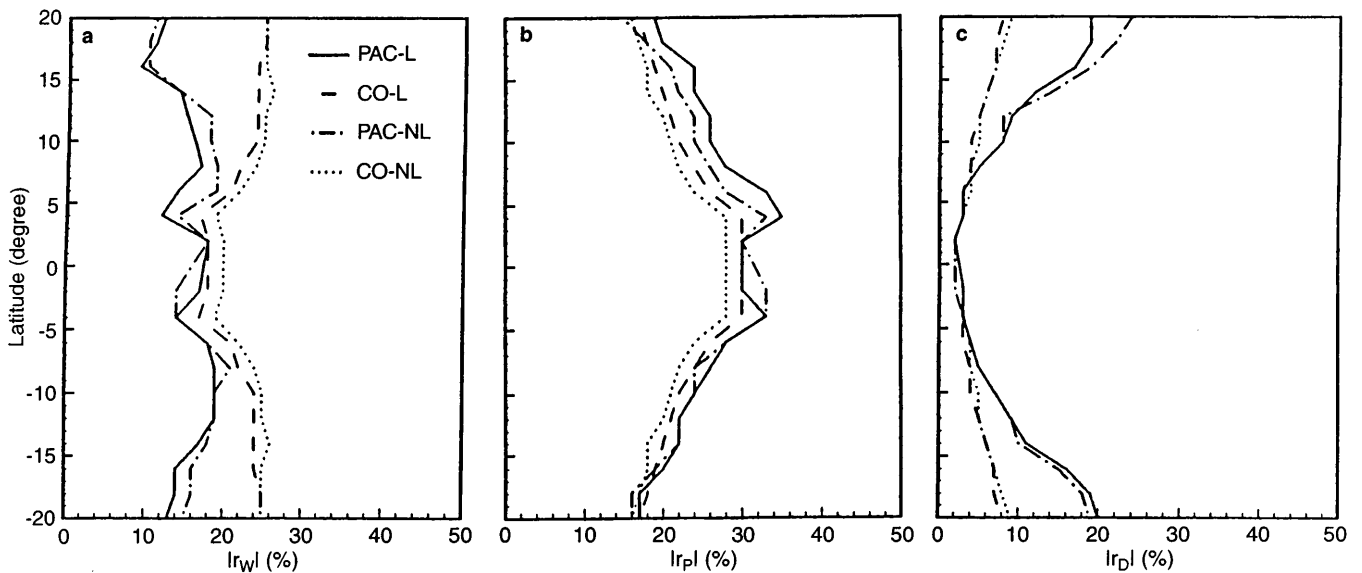


Fig. 2a-c. Energy flux coefficients (%) at different latitudes (degree). **a** r_W , **b** r_P and **c** r_D . Solid line: linear experiment with Pacific coastline (PAC-L). Dashed line: linear experiment with meridional coastline

(CO-L). Center-dashed line: non linear experiment with Pacific coastline (PAC-NL). Dotted line: non linear experiment with meridional coastline (CO-NL). Wave period: 60 days

fluxes do not present considerable differences; the smallest values are given when the coastline is meridional in the nonlinear model and the largest for the Pacific coastline in the linear model.

For an inclined boundary, it would be expected from inviscid theory, that the poleward propagation of coastal waves would be enhanced compared with the meridional boundary. However, as discussed in Soares *et al.* (1998), the dissipation induced by the inclined boundary is larger than that induced by the meridional one (see Fig. 2c). Hence, for the Pacific coastline the expected rise in poleward energy flux induced by the inclined boundary, is offset by dissipation.

The Pacific northward energy flux is a somewhat larger than the southward energy flux whereas the westward energy flux is smaller in the Northern Hemisphere than in the Southern Hemisphere (Fig. 2). This is consistent with the northern Pacific boundary being more nonmeridional (see Soares *et al.*, 1998). The Pacific energy dissipation is roughly similar in both hemispheres. Its westward energy flux presents a considerable latitudinal variation because of the changing coastline angle. This allows more than one critical latitude (in agreement with Grimshaw and Allen, 1988; Clarke and Shi, 1991; Clarke, 1992).

Furthermore, in Fig. 2a we note that the Pacific coastline is less reflective than the meridional boundary. This is expected because inclined boundaries favor trapped motion more than meridional ones.

Since the energy fluxes discussed are affected more by the coastline geometry than by the nonlinearities, hereafter only the linear cases are investigated.

3.2.2 Seasonal variability. To simulate the seasonal variability in the eastern Pacific ocean an equatorial Kelvin wave of 180 days period is used as an initial condition of the numerical model. The modelled region

in this experiment is from 45°S to 45°N and has a maximum longitudinal extent of 140° (see Fig. 1b for the boundary geometry).

The nondimensional energy flux and the energy dissipation coefficients generated at the Pacific coastline (PAC) are shown in Fig. 3 together with the energy fluxes generated at a meridional boundary (C0). The coefficients were calculated at every 5° of latitude and integrated over 6 months. The asymmetry between the Pacific Northern and Southern Hemispheres is small. Poleward of ~20° of latitude, the dissipation of energy is larger than the energy fluxes.

In agreement with the intraseasonal period experiment, the Pacific boundary is less reflective than the meridional boundary (Fig. 3a). The Pacific poleward energy flux (Fig. 3b) is slightly smaller than that generated at the meridional boundary because of the larger dissipation of energy occurring in the Pacific (Fig. 3c) and, thus, preventing the increase of poleward energy flux induced by the coastline geometry.

3.2.3 Annual variability. An equatorial Kelvin wave of 360 days period is used as an initial condition of the linear numerical model experiment. Following the previous case, the poleward energy flux and the dissipation of energy were numerically calculated for every 5° of latitude and integrated over 8 months. Since only half a wavelength is used as initial condition, it takes around 7 months of the integration period for all the poleward energy to leave the numerical domain.

The nondimensional energy fluxes and the nondimensional energy dissipation (PAC) are displayed in Fig. 4 together with the fluxes generated at the meridional boundary (C0).

In the northern Pacific, the westward energy flux differs substantially from that generated at the meridional boundary (Fig. 4a). Inviscid theory suggests that

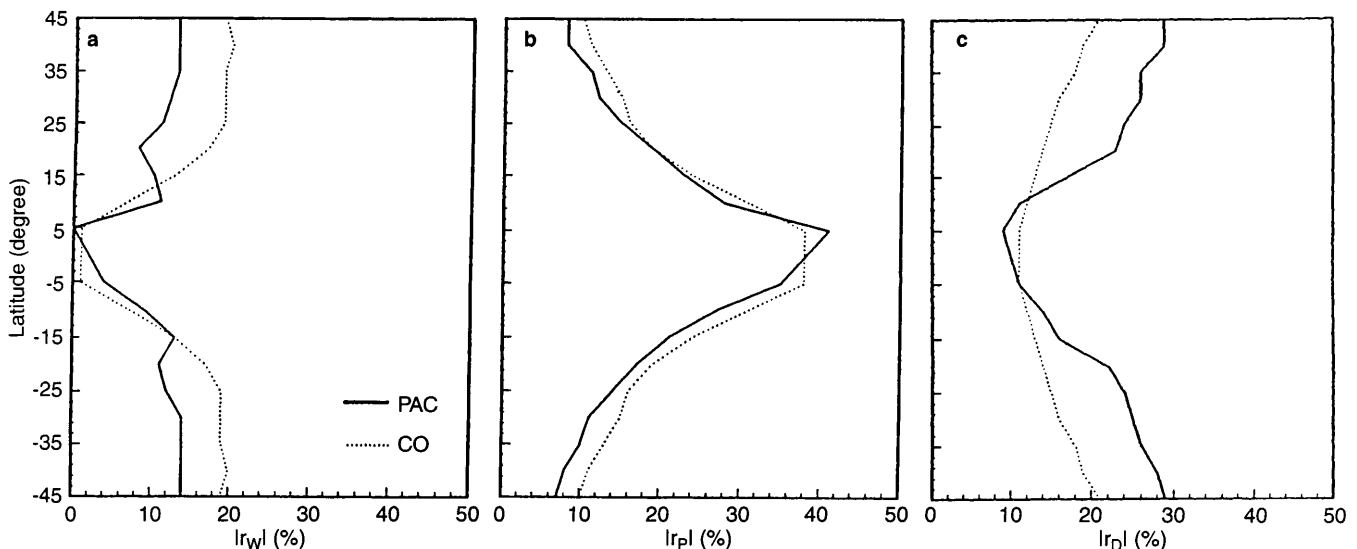


Fig. 3a–c. Linear energy flux coefficients (%) at different latitudes (degree). **a** r_W , **b** r_P and **c** r_D . Solid line: Pacific coastline (PAC). Dotted line: meridional boundary (C0). Wave period: 180 days

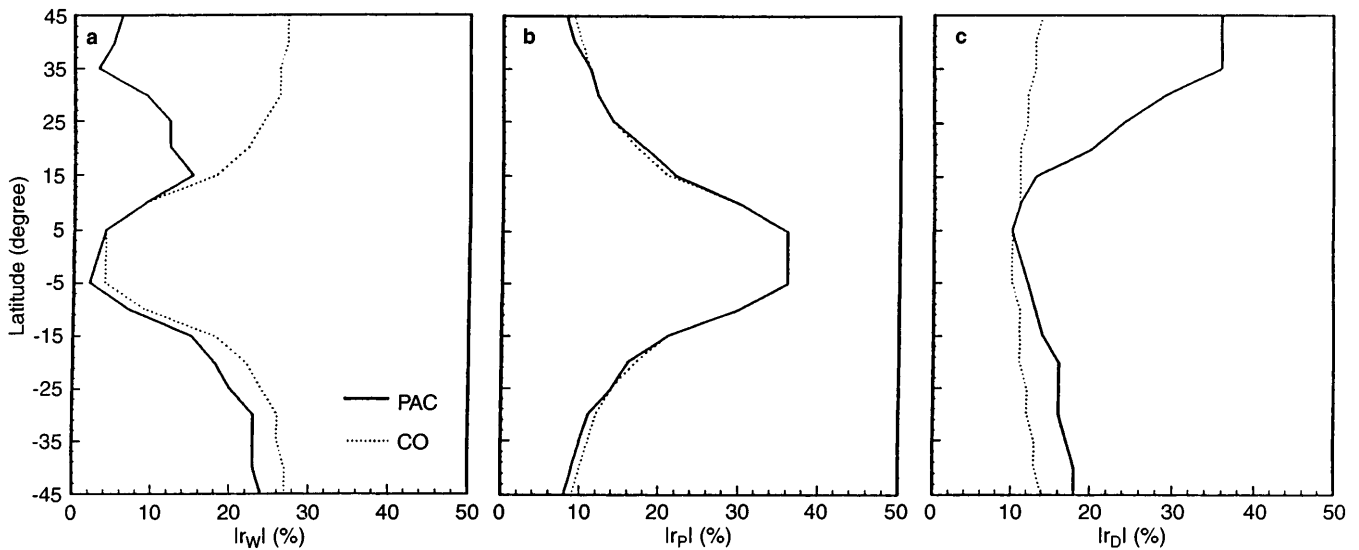


Fig. 4a–c. Linear energy flux coefficient (%) at different latitudes (degree). **a** r_W , **b** r_P and **c** r_D . Solid line: Pacific coastline (PAC). Dotted line: meridional boundary (CO). Wave period: 360 days

trapped motion is expected to be favored given that the northern Pacific coastline is less reflective than the meridional boundary, or than the southern Pacific coastline. However, from Fig. 4b, this is not the case. What happens is that the dissipation of energy (which increases as the boundary departs from the meridional direction; see Fig. 4c), restrains the increase in the northward energy flux induced by the coastline geometry.

The annual northward and southward energy fluxes, at the Pacific Ocean, are symmetric in relation to the equator (Fig. 4b). Above 20°N, the dissipation of energy is dominant over the energy fluxes. In the Southern Hemisphere, however, the coastline geometry facilitates the boundary reflection and, poleward of 20°S, the westward energy flux is larger than the dissipation of energy. In the south Pacific, the energy fluxes and the

energy dissipation are not substantially different from those generated in the meridional boundary experiment. This is because the southern Pacific coastline does not depart significantly from the north-south direction.

3.2.4 Discussion. Figure 5 summarizes the energy fluxes and the energy dissipation coefficients obtained for the Pacific Ocean at intraseasonal (T60), seasonal (T180) and annual (T360) periods. The intraseasonal coefficients were calculated only up to 20° of latitude and therefore a direct comparison between the intraseasonal coefficients and the lower frequency coefficients should be made with prudence.

The energy fluxes are strongly dependent on the energy dissipated in the domain, as shown by Soares

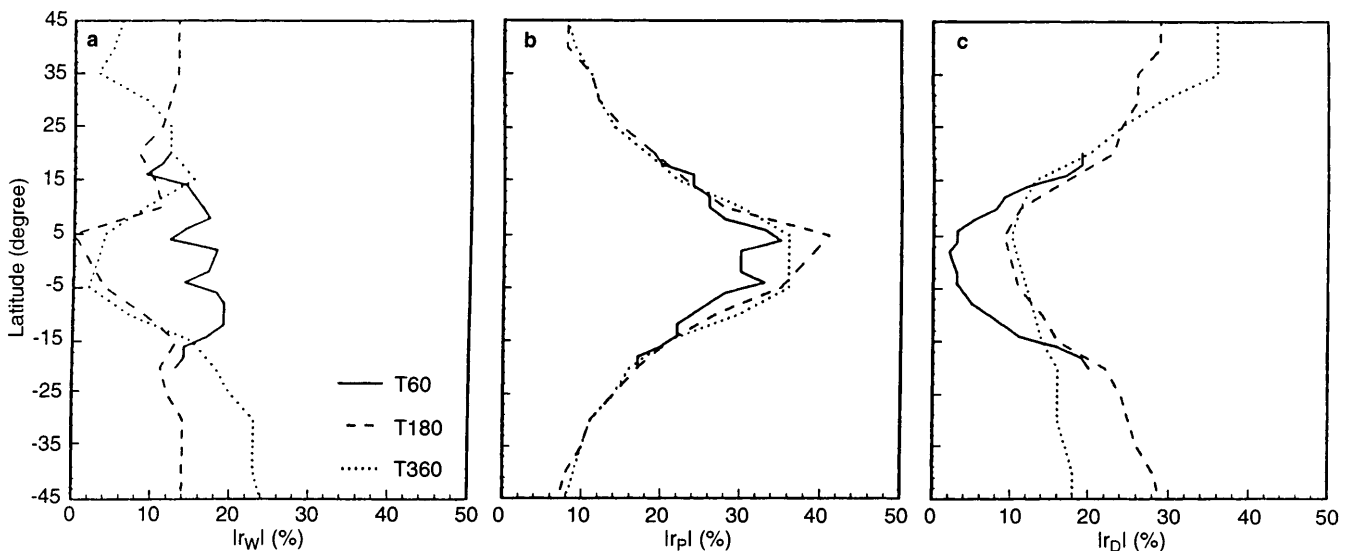


Fig. 5a–c. Linear energy flux coefficients (%) at different latitudes (degree) for different incident wave periods. **a** r_W , **b** r_P and **c** r_D . Pacific boundary

et al. (1998). In the Southern Hemisphere, the dissipation of energy is smaller in the annual experiment than in the seasonal one (Fig. 5c). This is explained by the critical latitude values being higher for the annual experiment. Therefore, the increase in dissipation due to the increase of wave period is shown to be less important than the energy dissipated by the presence of coastal Kelvin waves. In the Northern Hemisphere, however, the energy dissipated in the annual case is larger than that for the seasonal case. This is, probably, due to the combination of both factors, the presence of the coastal Kelvin waves in the domain and the increase in the wave period.

The intraseasonal (T60) values of r_W (Fig. 5a) and r_D (Fig. 5c) are, respectively, larger and smaller than those obtained by the lower frequency experiments.

The westward energy flux, in the Southern Hemisphere, is larger for the annual period experiment (T360) than for the seasonal period (T180) case. In the Northern Hemisphere (where the boundary is more nonmeridional) the comparatively larger presence of coastal Kelvin waves, in the annual period experiment, induces stronger dissipative effects (see Fig. 5c) inhibiting the reflection processes. As a result, less energy of annual period is leaked offshore (Fig. 5a). According to inviscid studies (Clarke and Shi, 1983; Clarke, 1992) the poleward energy flux decreases and the westward energy flux increases as the incident Kelvin wave period is increased. However, calculations for the intraseasonal, seasonal and annual frequencies all indicate that the coastally trapped energy flux, poleward of 15° , does not depend significantly on the period of the incident wave (Fig. 5b).

In contrast to inviscid theory, there is symmetry between the northward and southward energy fluxes for all frequencies. The symmetry of r_P can be accounted for the larger dissipative effects in the Northern Hemisphere

which compensates for the increase of the northward energy flux generated by the coastline geometry, and hence results in similar r_P values for both hemispheres.

The hemispherical asymmetry of both, westward energy flux and energy dissipation, is greater for the annual experiment. This result is in agreement with Clarke (1992) who found that the energy flux asymmetry in the eastern Pacific increases as the wave period increases.

3.3 Model Atlantic Ocean results

The experiments carried out for the eastern Pacific Ocean coastline are now repeated for the eastern Atlantic Ocean coastline. The methodology employed is similar to that utilized in the previous experiment.

The Atlantic coastline geometry can be seen in Fig. 1c (intraseasonal period) and 1d (seasonal and annual periods).

3.3.1 Intraseasonal variability. The intraseasonal nondimensional linear and non linear energy flux coefficients, $r_P(\gamma, T)$, $r_W(\gamma, T)$ and $r_D(\gamma, T)$ generated at both, Atlantic boundary and meridional boundary, are shown in Fig. 6 at different latitudes. The coefficients are calculated at latitudinal intervals of 2° and integrated over 90 days. The energy coefficients are calculated using the: (1) Atlantic coastline and the linear model (ATL-L); (2) meridional coastline and the linear model (CO-L); (3) Atlantic coastline and the non linear model (ATL-NL) and (4) meridional boundary and the non linear model (CO-NL).

In agreement with the earlier experiments, the energy flux changes induced by the coastline geometry are significantly more important than those induced by nonlinearities (Fig. 6).

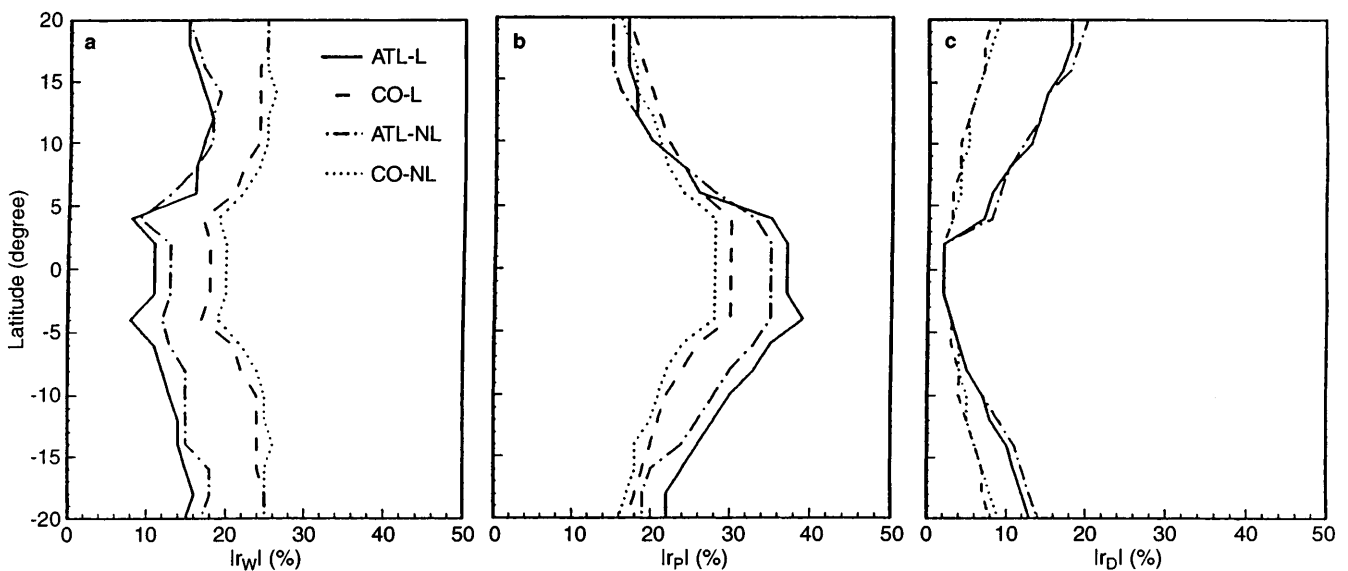


Fig. 6a–c. Energy flux coefficient (%) at different latitudes (degree). **a** r_W , **b** r_P and **c** r_D . Solid line: linear experiment with Atlantic coastline (ATL-L). Dashed line: linear experiment with meridional coastline (CO-L). Center-dashed line: non linear experiment with Atlantic coastline (ATL-NL). Dotted line: non linear experiment with meridional coastline (CO-NL). Wave period: 60 days

(CO-L). Center-dashed line: non linear experiment with Atlantic coastline (ATL-NL). Dotted line: non linear experiment with meridional coastline (CO-NL). Wave period: 60 days

Near the Gulf of Guinea, the reflected energy flux and the dissipated energy, both exhibit a rapid increase whereas the poleward energy flux shows a rapid decrease. The rise in the r_D value is due to the energy dissipated along the zonal boundary (see Fig. 6b). The larger amount of dissipation reduces the northward energy flux.

The Atlantic coastline is shown by Fig. 6a to be less reflective than the meridional one. This result is theoretically expected (Soares *et al.*, 1998) given that the critical latitudes for the nonmeridional boundaries are lower than those generated at the meridional coastlines.

For all the cases examined in Fig. 6b, north of 5°N , the northward energy fluxes are similar, and hence, poleward of 5°N , the Northern Atlantic coastline acts as a meridional boundary. In the Southern Hemisphere, the poleward energy generated in the Atlantic coastline is larger than that generated at the meridional boundary. In agreement with the earlier experiments the energy dissipation induced by the nonmeridional boundary (Atlantic coastline) is larger than that induced by the meridional one (Fig. 6c). The increase in dissipation reduces the expected rise in the poleward energy flux induced by the geometry of the coastline.

3.3.2 Seasonal variability. To compare the energy flux changes induced by the coastline geometry, the Atlantic energy flux coefficients (ATL) are shown in Fig. 7 with the corresponding fluxes generated at the meridional boundary (C0). The coefficients are calculated at every 5° of latitude and integrated over 6 months. The asymmetry between the Northern and Southern Hemispheres is found to be negligible for all the seasonal energy fluxes investigated here. It indicates that the geometrical effects of the Gulf of the Guinea are not very important for seasonal period motions.

As for the intraseasonal period experiment, the Atlantic boundary is less reflective than the meridional boundary (see Fig. 7a). According to Fig. 7b, with respect to the seasonal poleward energy flux the whole eastern Atlantic boundary can be roughly regarded as a meridional boundary. Again, the comparatively larger energy dissipated at the Atlantic boundary (Fig. 7c) obstructs the expected increase of poleward energy flux induced by the coastline geometry.

3.3.3 Annual variability. To compare the coastline influences on the energy fluxes and on the energy dissipation, the nondimensional coefficients generated by the Atlantic coastline (ATL) and by a meridional boundary (C0) are displayed together in Fig. 8. In common with the seasonal experiment, all the annual energy coefficients, generated at the Atlantic eastern coast, are approximately symmetric with respect to the equator.

The annual poleward energy fluxes induced by both, meridional and Atlantic boundaries, are very similar. As expected, the energy dissipated (Fig. 8c) and the reflected flux (Fig. 8a) are, respectively, larger and smaller at the Atlantic boundary compared with the meridional boundary.

3.3.4 Discussion. The intraseasonal, seasonal and annual energy fluxes and energy dissipation coefficients are summarized in Fig. 9. In agreement with Fig. 5 the westward energy flux is larger for the intraseasonal period than for longer periods (Fig. 9a). This is because of the lower values of energy dissipated, in the domain, at the intraseasonal period (Fig. 9c).

As the wave period increases, from seasonal to annual, the reflected energy increases (Fig. 9a) and the dissipation of energy decreases (Fig. 9c) because of the

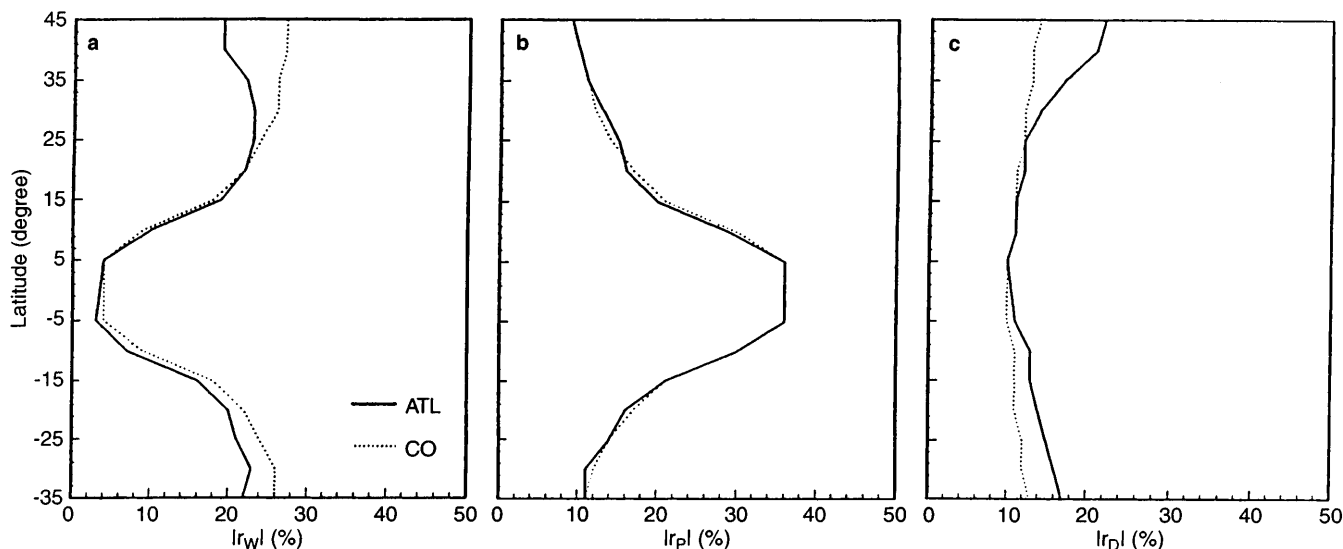


Fig. 7a–c. Linear energy flux coefficient (%) at different latitudes (degree). **a** r_W , **b** r_P and **c** r_D . Solid line: Atlantic coastline (ATL). Dotted line: meridional boundary (C0). Wave period: 180 days

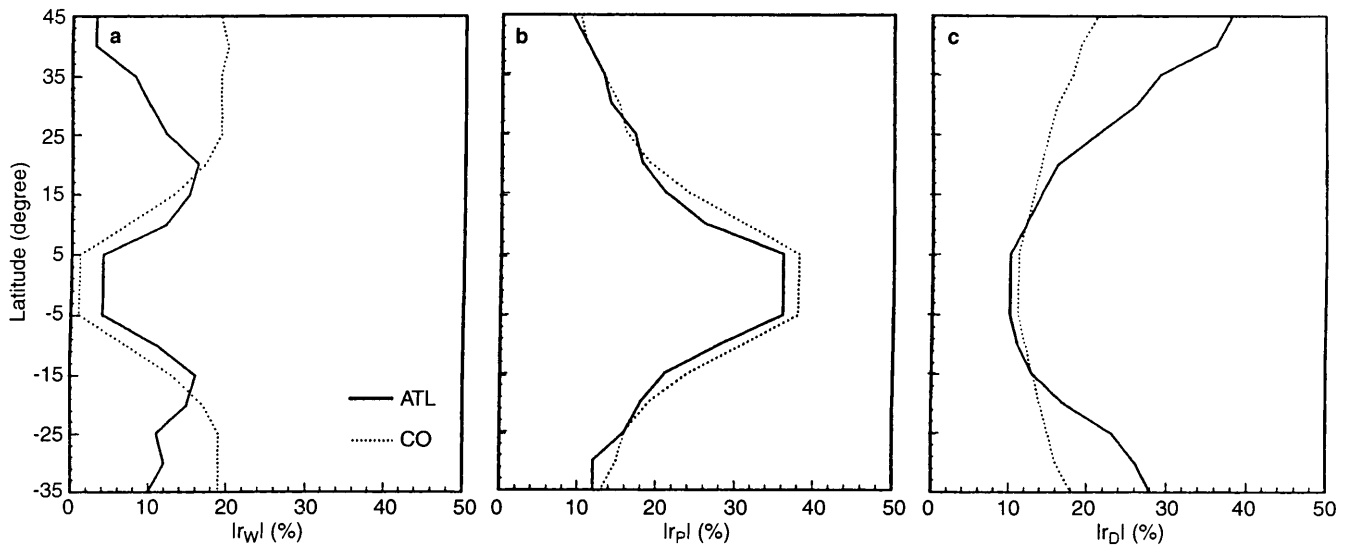


Fig. 8a–c. Linear energy flux coefficient (%) at different latitudes (degree). **a** r_W , **b** r_P and **c** r_D . Solid line: Atlantic coastline (ATL). Dotted line: meridional boundary (CO). Wave period: 360 days

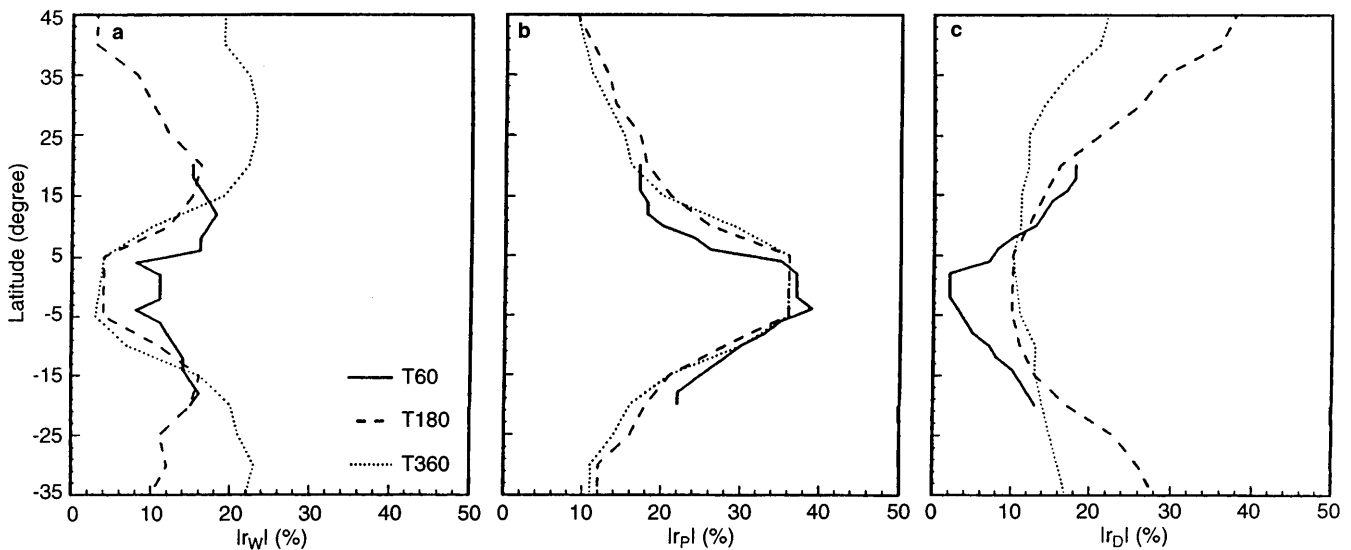


Fig. 9a–c. Linear energy flux coefficient (%) at different latitudes (degree) for different incident wave periods. **a** r_W , **b** r_P and **c** r_D . Atlantic boundary

increase of the critical latitude with the lengthening of the wave period. As the critical latitude increases, there is more energy in the westward Rossby waves and, consequently, smaller amount of energy dissipated in the domain.

It is found that the seasonal and the annual poleward energy fluxes are very similar (Fig. 9b). Both fluxes are also comparable to the poleward energy flux generated at the meridional boundary (see Figs. 7b, 8b). Despite the reflected energy being smaller for the seasonal case than for the annual experiment, the seasonal energy dissipated in the domain is larger, resulting in similar values of the poleward energy fluxes for both periods.

The influence of the Atlantic coastline geometry, therefore, on the seasonal and annual coastally trapped

energy flux can be considered to be small. This result is striking because of the particular geometry of the eastern Atlantic, which has an approximately zonal coast near 5°N (Gulf of the Guinea). Du Penhoat *et al.* (1983) have also shown that the effect of the coast of the Gulf of Guinea is small on very low frequency waves (seasonal and annual periods).

The largest asymmetry between the Northern and Southern Hemisphere energy fluxes has been found in the intraseasonal experiment. At intraseasonal periods the effects of the Atlantic coastline geometry are to cause an enhancement of the poleward energy flux and a reduction in Rossby waves generation, between 20°S and 5°N. The flow produced by the coastal Kelvin wave along of the approximately zonal boundary of the Gulf of Guinea also contributes to this result.

4 Conclusions

The effect of the coastline geometry and the incident wave period (intraseasonal, seasonal and annual periods), was found to be more important for the westward energy flux than for the poleward flux. To simulate accurately the reflected Rossby waves on the Pacific and Atlantic boundaries, the eastern ocean coastline geometry should be included in the numerical models.

The effect of the inclination of the eastern boundary on the poleward energy flux, for the Pacific and Atlantic oceans, diminishes as the period of the incident wave increases. For motions of seasonal and annual periods, the influence of the coastline inclination, on both oceans, can be considered negligible.

For incident waves of intraseasonal period, however, there is a poleward energy flux asymmetry between the Northern and Southern Hemispheres. For the Northern Atlantic, poleward of 5°N, the eastern boundary can be considered as a meridional one whereas for the Southern Atlantic the eastern coastline geometry should be incorporated to obtain accurate poleward propagation of intraseasonal period. In the Pacific Ocean, the northward energy flux was found to be somewhat larger than the northward flux generated at a meridional boundary. In the Southern Hemisphere, the difference between the poleward fluxes, of intraseasonal period, generated at the meridional and the Pacific coastlines, however, are considered negligible.

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